

Analysis algorithm/datastructure

memory/CPU/operations  $O(n)$  Notation

Queues FIFO add-to-rear / take-from-front enqueue/dequeue  $O(1)$   
array-based (circular array) / linked-list-based

Stack LIFO add/take-from-top array-based/linked-list-based

⇒ resize array when full, doubling-strategy

Singly-Linked-List H → [ ] → [ ] → [ ] → NULL

⇒ Sequence ADT  
⇒ List

Doubly-Linked-List H → [ ] ↔ [ ] ↔ [ ] ← T

Vectors extended concept of array, resizes as needed

Trees traversal: pre, in, post-order root, nodes, leaves  
depth → node, height → tree subtrees

- Binary Tree: 2 children per node, ordered (left/right)
- Heap: binary tree, internal nodes store keys,  $Key(n) \geq Key(\text{parent}(n))$   
also called Heap-Order, complete binary tree,  $\log(n)$

Insertion ⇒ Upheap: restore order, swap val upward till root or  $n > \text{val}$

Removal ⇒ replace root with last node, make last node leaf  
Downheap: restore order, swap with child and repeat

Max-Heap:  $\geq$ , large num at root, Min-Heap:  $\leq$ , smallest num at root

- BST (Binary Search Tree): binary tree where  $Key(l) \leq Key(p) \leq Key(r)$   
 $\log(n)$  find/search, needs to be balanced for efficiency
- (2,4)-Tree: Multi-Way Search Tree, internal nodes store (d-1) ele  
where d is the num. of children, ordered as BST, split/fusion
- AVL-Tree: balanced BST, height of all subtrees may only differ by -1,

~~if root.bal < -2: (if R.bal < 0: (RL(root); if == -1: RL(R);) elif == 1: RR(R); RL(root);)~~  
if root.bal < -2: (if R.bal < 0: (RL(root); if == -1: RL(R);) elif == 1: RR(R); RL(root);)

Tree/Node rotations: RIGHT(r):  
p = r → left;  
r → left = p → right;  
p → right = r;  
reset parent to p;

LEFT(r):  
p = r → right;  
r → right = p → left;  
p → left = r;  
reset parent to p;

if root.bal:  
analog, but  
inverting  
directions,  
signs and

Sorting:

- Heap-Sort: use a priority queue implemented as heap,  $O(n \log(n))$   
add all you want to sort, remove  $\min()$  (the root,  $\max()$ )

$O(n \log(n))$   
expected  
 $O(n^2)$  we

- Quick-Sort: divide-and-conquer, divide by picking a pivot, putting everything less before, bigger after, and repeat/recurse on the left and right partitions, at the end; join back together

$O(n \log(n))$

- Merge-Sort: divide-and-conquer, divide until small and easy to sort, then join the pieces back, merging them

$O(n)$

- Bucket-Sort: if "spread" of elements known, we first prepare a sorted list of buckets and throw in the elements,

$O(n)$

then take them out again (counting-sort similar for integers)

$O(n)$

- Radix-Sort: lexicographic-sort using bucket-sort

Priority-Queues: queue where elements have a priority, ordered by priority (maintaining FIFO order too), heap OK, usually remove  $\min()$

Hash-Tables: array, map into it with hash-function,  $O(1)$  lookup if good, random hash-function, either closed-addressing  $\Rightarrow$  chains (Linear Probing) of max size, then double array, or open-addressing  $\Rightarrow$  rehash or try

Dictionary: lookup of elements, BST (balanced) or HT or Skip-List

Graphs: Vertices, Edges; directed/undirected; degree, path, cycle

Digraph: directed graph, DFS/BFS, topological sorting

DFS (Depth-First Search):

BFS (Breadth-First Search):

Shortest Paths: Dijkstra (not-negative-weights), Bellman-Ford (also negative), DAG-based, All-Pair SP

Minimum Spanning Tree: Prim-Jarnik, Kruskal